# MATH 402 Midterm 1 Practice <br> Wednesday 26 September, 2018 

Prove or find a counterexample for each of the following statements. (On the true/false portion of the exam you will not be asked for proofs, but this is much better practice, for all parts of the exam.)

|  |  | True | False |
| :---: | :---: | :---: | :---: |
| (a) | SSA congruence is a theorem in Hilbert's axiomatic system. |  | F |
| (b) | Let $c$ be a Euclidean circle. Suppose that $P$ and $Q$ are two points such that the power of each with respect to $c$ is equal to $\frac{1}{2}$. Then the segment from $P$ to $Q$ does not intersect the boundary of the circle. |  | F |
| (c) | In neutral geometry, the angles of an equilateral triangle are always $60^{\circ}$. |  | F |
| (d) | Euclid's favourite thing about his axiomatic system was that he could prove that all of the axioms were mutually independent. |  | F |
| (e) | In Euclidean geometry, if $\ell_{1}$ and $\ell_{2}$ are two unequal parallel lines, and $m$ is another line which intersects $\ell_{1}$ (but is not equal to $\ell_{1}$ ), then $m$ must intersect $\ell_{2}$. | T |  |
| (f) | Let $A$ and $B$ be two distinct points. A third point $C$ is of equal distance from both $A$ and $B$ if and only if $C$ lies on the perpendicular bisector of the segment $\overline{A B}$. | T |  |
| (g) | We need to use the Parallel Postulate (or Playfair's Postulate) to make sense of the notion of two points being on the same side or on opposite sides of a line. If we don't have the Parallel Postulate, this notion doesn't make sense. |  | F |
| (h) | An inscribed angle $\angle A B C$ is one where the vertex $B$ lies on the minor arc determined by the points $A$ and $C$. |  | F |
| (i) | In neutral geometry, a line which is perpendicular to one of two parallel lines is also perpendicular to the other. |  | F |
| (j) | Let $c$ and $c^{\prime}$ be two circles with centres $O$ and $O^{\prime}$ respectively. Assume that they intersect at a point $T$ and that there is a line through $T$ which is tangent to both $c$ and $c^{\prime}$. Then the point $T$ lies on the line $\overleftrightarrow{O O^{\prime}}$. | T |  |
| (k) | Let $c$ be a (Euclidean) circle, and assume that $P$ and $Q$ are two distinct points of $c$. Then the inverse of $P$ with respect to $c$ can never be equal to the inverse of $Q$ with respect to $c$. | T |  |
| (1) | $x^{2}+2 y^{2}=4$ is the equation of a (Euclidean) circle. |  | F |
| (m) | Given a triangle $\triangle A B C$, let $D$ be the midpoint of $\overline{A B}$ and let $E$ be the midpoint of $\overline{A C}$. Then $D E=\frac{1}{2} B C$. | T |  |

