Thursday, April 4 ** Surface Parameterpalooza

- 1. Let *S* be the portion of the plane x + y + z = 1 which lies in the positive octant.
 - (a) Draw a picture of *S*.
 - (b) Find a parameterization $\mathbf{r} \colon D \to S$, being sure to clearly indicate the domain D. Check your answer with the instructor.
- 2. Consider the surface *S* which is the part of $z + x^2 + y^2 = 1$ where $z \ge 0$.
 - (a) Draw a picture of *S*.
 - (b) Find a parameterization $\mathbf{r} \colon D \to S$. Check your answer with the instructor.
- 3. Let *S* be the surface given by the following parameterization. Let $D = [-1,1] \times [0,2\pi]$ and define

$$\mathbf{r}(u,v) = (u\cos v, u\sin v, v).$$

- (a) Consider the vertical line segment $L = \{u = 0\}$ in D. Describe geometrically the image of L under \mathbf{r} .
- (b) Repeat for the vertical segments where u = -1 and u = 1.
- (c) Use your answers in (a) and (b) to make a sketch of *S*.
- 4. Consider the ellipsoid *E* given by $\frac{x^2}{9} + \frac{y^2}{4} + z^2 = 1$.
 - (a) Draw a picture of *E*.
 - (b) Find a parameterization of E. Hint: Find a transformation $T: \mathbb{R}^3 \to \mathbb{R}^3$ which takes the unit sphere S to E, and combine that with our existing parameterization of the plain sphere S.