

### Useful R commands

- The R command to perform an one sample  $t$ -test for the hypotheses:  $H_0 : \mu = \mu_0$  against  $H_1 : \mu \neq \mu_0$  is

```
t.test(x,mu=mu0,alternative=".").
```

The alternative can be `greater`, `less` and `two.sided`.

This command produces the test statistic, the  $p$ -value and a 95% CI for  $\mu$  (default is  $\alpha = 0.05$ ). If  $(1 - \alpha)\%$  CI is needed, one should set `alpha=0.xx` and add “`conf=1-alpha`” to `t.test`, that is

```
alpha=0.xx  
t.test(x,mu=mu0,alternative=".",conf=1-alpha)
```

- The R command for  $k$  such that  $\Pr(t_{n-1} < k) = p$  is `qt(p,n-1)`.
- The R commands for calculating sample mean and sample standard deviation for `x` are

```
smean=mean(x)  
ssd=sd(x)
```

### Important points

- You will read data from the course website.
- You will perform suitable tests on the data.
- You will calculate rejection region and compare the sample mean to draw your decision of the test.

### Practice Problems

Open the data set `survey` containing measurements of the following variables from 95 students:

sex	1=male; 2=female
age	Year
height:	Inches
credit:	Number of credit cards in possession
pulse:	Number of heartbeats in one minute
pulse.ex:	Number of heartbeats in one minute after regular exercise over a period
exercise:	Number of hours of exercise last week
smoke:	1=yes; 2=no
hand:	1=left-handed; 2=right-handed; 3=ambidextrous

Read the data `survey`. Set `pulse.sf` to contain the `pulse` among female students who smoke.

```
survey=read.csv("http://rome/u/UG/IM/STAT2012/r/survey.csv")
attach(survey)
pulse.sf=pulse[smoke==1 & sex==2]
pulse.sf
```

1. Test if the mean of the pulse among female students who smoke (`pulse.sf`) is 70 or more than 70.

- (a) State the null and alternative hypotheses.
- (b) Draw a *qq-plot* of the data and comment the normality assumption of the data.
- (c) Find the sample mean named as `smean` and sample standard deviation named as `ssd` of the pulse among female students who smoke (`pulse.sf`).
- (d) Perform a suitable test. Report the test statistic and *p*-value. Draw your conclusion about the null hypothesis regarding the mean of the pulse among female students who smoke based on the *p*-value.
- (e) State the rejection region for the sample mean when the level of significance is  $\alpha = 0.05$ . Draw your conclusion about the null hypothesis based on the rejection region.

```
n=length(pulse.sf)
n
cv=qt(0.95,n-1)
cv
mu0=70
rr.bound=mu0+cv*ssd/sqrt(n)
rr.bound
```

- (f) Using the test result of (d), state the one-sided 95% confidence interval for the true mean. Draw your conclusion about the null hypothesis based on the confidence interval.
- (g) Do the three ways of testing the hypotheses, in (d), (e) and (f), give consistent result?